

Rational Exponents:

Rational #'s: #'s that can be written as a fraction

Rational Exponent: exponent written as fraction

$x^{\frac{n}{m}}$
↑
base

→ power: how many times to multiply base

→ root: a # that multiplies that many times to get base ($m \geq 1$)

writing expo form to radical form

$$x^{\frac{n}{m}} \Rightarrow \sqrt[m]{x^n} \Rightarrow \left(\sqrt[m]{x}\right)^n$$

expo form radical form

example:

$\sqrt{\quad}$ = understood square root

$$4^{3/2} = \sqrt{4^3} = (\sqrt{4})^3$$
$$= 8 \quad = 8 \quad = 8$$

Expo form to radical form

$$(4x^5y^7)^{1/9} = \sqrt[9]{4x^5y^7}$$

$$(2x^3y^4)^{2/5}$$

$$2^{2/5} x^{6/5} y^{8/5} = \sqrt[5]{2^2 x^6 y^8}$$

radical form to expo form

$$\sqrt[6]{7^5 x^3 y^9} = 7^{5/6} x^{3/6} y^{9/6}$$
$$7^{5/6} x^{1/2} y^{3/2}$$

$$\sqrt[4]{16x^5y^8z^{13}} = 16^{1/4} x^{5/4} y^{8/4} z^{13/4}$$
$$\boxed{2x^{5/4}y^2z^{13/4}}$$

Simplifying

ex: $(x^{\frac{2}{3}} y^{\frac{1}{3}})(2x^{\frac{9}{2}} y^{\frac{8}{3}})$

$$2x^{\frac{4}{2}} y^{\frac{9}{3}} = 2x^2 y^3$$

ex: $(8x^8 y^{-15})^{\frac{1}{3}}$

$$8^{\frac{1}{3}} x^{\frac{8}{3}} y^{-5} = \frac{2x^{\frac{8}{3}}}{y^5}$$

write in simplest radical form

ex: $(2^5 x^8 y^{16})^{\frac{1}{5}}$

$$\sqrt[5]{2^5 x^8 y^{16}} \quad \begin{array}{l} 5 \overline{) 8} \\ \underline{-5} \\ 3 \text{ inside} \end{array} \quad \begin{array}{l} 1 \text{ outside} \end{array}$$

$$2xy^3 \sqrt{x^3 y}$$

• write in simplest radical form

$$(6x^4 y^5 z^{11})^{\frac{1}{3}}$$

$$= \sqrt[3]{6x^4 y^5 z^{11}}$$

$$\boxed{x^1 y^1 z^3 \sqrt[3]{6x^1 y^2 z^2}} \quad \begin{array}{l} 3 \overline{) 11} \\ \underline{-9} \\ 2 \text{ in} \end{array} \quad \begin{array}{l} 3 \text{ out} \end{array}$$

$$(2^7 x^9 y^{15} z^{23})^{\frac{1}{5}}$$

$$= \sqrt[5]{2^7 x^9 y^{15} z^{23}}$$

$$\boxed{2xy^3 z^4 \sqrt[5]{2^2 x^4 z^3}}$$

Equations with rational exponents

ex: $x^{\frac{3}{2}} - 8 = 19$

$$\sqrt[3]{x^3} = \sqrt[3]{\#} = \frac{1}{3}$$

$$x^{\frac{3}{2} + \frac{2}{3}} = (27)^{\frac{2}{3}}$$

$$(\sqrt{x})^2 = \#^2$$

$$x = 9$$

$$\Rightarrow \sqrt[3]{27} = 3^2 = 9$$

ex: $2x^{\frac{5}{2}} - 8 = 56$

$$x^{\frac{5}{2} + \frac{2}{5}} = 32^{\frac{2}{5}}$$

$$2x^{\frac{5}{2}} = 64$$

$$x = 4$$

simplest radical form

ex:

$$\sqrt[3]{\frac{4x^8y^{21}z^4}{2^2z^3z^1}}$$

$$\sqrt[3]{\frac{4}{1}}$$

$$x^2y^7z \sqrt[3]{4x^2z}$$

Solving equations with rational exponents

ex:

$$x^{\frac{2}{3}} + 4 = 20$$

$$\left(\sqrt[3]{x}\right)^3$$

$$\left(x^{\frac{2}{3}}\right)^{\frac{3}{2}} = (16)^{\frac{3}{2}}$$

$$\sqrt{x^2} = (x^2)^{\frac{1}{2}}$$

$$x = 64$$

ex:

$$2x^{\frac{5}{2}} - 8 = 56$$

$$\frac{2x^{\frac{5}{2}}}{2} = \frac{64}{2}$$

$$x^{\frac{5}{2}} = 32$$

$$x = 4$$